

Summary

- Nonparametric tests do not make assumptions that the population is from a specific distribution. Therefore its results are more robust than a parametric test when such assumptions are violated.
- Nonparametric tests are often used in place of their parametric counterparts when certain assumptions about the underlying population are questionable.
- The sign test is the simplest of the nonparametric tests, and is similar to testing if a two-sided coin is fair. Its name comes from the fact that it is based on the direction (or signs for pluses and minuses) of a pair of observations and not on their numerical magnitude.
- The One Sample Sign Test is a nonparametric equivalent to the parametric One Sample t-Test.
- The one-sample sign test is used to test the null hypothesis that the probability of a random value from the population being above the specified value is equal to the probability of a random value being below the specified value.
- Sign test make null hypothesis about true median
- If null hypothesis is true, S should have binomial distribution with success probability .5
- To test $H_0: M=M_0$ against the alternative hypothesis $H_1: M \neq M_0$ where M_0 is the given value of the population median, Compute $P(X \leq U) = \sum_{c_x}^U n_{c_x} \left(\frac{1}{2}\right)^x \left(\frac{1}{2}\right)^{n-x}$ and this value is compared with $\alpha/2$, the level of significance. If the calculated value of $P(X \leq U)$ is less than the predicted $\alpha/2$, the null hypothesis is rejected where U is the number of positive signs
- If $n \geq 25$, the value of Z is computed and the normal test is applied to decide about H_0 where

$$Z = \frac{(U + 0.5) - np_0}{\sqrt{np_0(1 - p_0)}} \quad \text{when } U < np_0$$

$$Z = \frac{(U - 0.5) - np_0}{\sqrt{np_0(1 - p_0)}} \quad \text{when } U > np_0 \text{ where } p_0 = 0.5$$

