

Summary

- A confidence interval for variance gives an estimated range of values which is likely to include an unknown population variance, the estimated range being calculated from a given set of sample data
- The confidence level is the probability value $(1 - \alpha)$ associated with a confidence interval which is often expressed as a percentage
- 100 (1- α) % C.I for the population variance σ^2 when the mean is known as μ is given by

$$\begin{aligned} & \circ [\sum(y_i - \mu)^2 / B, \sum(y_i - \mu)^2 / A] \text{ where } B = \chi_{\alpha/2}^2(n) \text{ and} \\ & \circ A = \chi_{(1-\alpha/2)}^2(n) \end{aligned}$$

- 100 (1- α) % C.I for the population variance σ^2 when the mean is unknown is given by

$$\begin{aligned} & \circ [\sum(y_i - \bar{y})^2 / B, \sum(y_i - \bar{y})^2 / A] \text{ where } B = \chi_{\alpha/2}^2(n-1) \text{ and} \\ & \circ A = \chi_{(1-\alpha/2)}^2(n-1) \end{aligned}$$

- 100 (1- α) % C.I for the ratio of variances of two populations with unknown means is given by

$$\begin{aligned} & \left[\frac{s_1^2}{Bs_2^2}, \frac{s_1^2}{As_2^2} \right] \text{ where } B = F_{\alpha/2}(m-1, n-1) \text{ and} \\ & A = F_{(1-\alpha/2)}(m-1, n-1) \end{aligned}$$

- 100 (1- α) % confidence interval for the ratio of variances when the respective means are known is computed as

$$\begin{aligned} & \left[\frac{n \sum_{i=1}^m (x_i - \mu_1)^2}{Bm \sum_{i=1}^n (y_i - \mu_2)^2}, \frac{n \sum_{i=1}^m (x_i - \mu_1)^2}{Am \sum_{i=1}^n (y_i - \mu_2)^2} \right] \text{ where } B = \\ & F_{\alpha/2}(m, n) \text{ and } A = F_{(1-\alpha/2)}(m, n) . \end{aligned}$$