

Summary

- Measures of variability can help one to create a mental picture of the spread of the data
- Sometimes a population variance σ^2 is the primary objective in an experimental investigation
- If the assumptions are met, $(s_1^2 / \sigma_1^2) / (s_2^2 / \sigma_2^2)$ follows a distribution known as the *F distribution* with *two* values used for degrees of freedom
- A confidence interval for the ratio of variances gives an estimated range of values, which is likely to include a ratio of unknown population variances, the estimated range being calculated from a given set of sample data
- The confidence level is the probability value $(1-\alpha)$ associated with a confidence interval which is often expressed as a percentage
- 100 $(1-\alpha)$ % C.I for the ratio of variances of two populations with known means as μ_1 and μ_2 is given by

$$\left[\frac{n \sum_{i=1}^m (x_i - \mu_1)^2}{Bm \sum_{i=1}^n (y_i - \mu_2)^2}, \frac{n \sum_{i=1}^m (x_i - \mu_1)^2}{Am \sum_{i=1}^n (y_i - \mu_2)^2} \right]$$

Where, $B = F_{\alpha/2}(m, n)$ and $A = F_{(1-\alpha/2)}(m, n)$

- 100 $(1-\alpha)$ % C.I for the ratio of variances of two populations with unknown means is given by

$$\left[\frac{s_1^2}{Bs_2^2}, \frac{s_1^2}{As_2^2} \right]$$

Where, $B = F_{\alpha/2}(m-1, n-1)$ and $A = F_{(1-\alpha/2)}(m-1, n-1)$