

Summary

- An estimator or estimate is said to be a best estimator or estimate if it is unbiased, consistent, efficient and sufficient
- The amount of bias: $B = \text{Estimated value} - \text{True value of the parameter}$
- The sample mean \bar{x} is an unbiased estimator of the population mean
- Unbiased estimator of the population variance in case of Normal population is given by $n s^2 / (n-1)$
- An estimator is said to be consistent if the variance of its sampling distribution decreases with increasing sample size
- An estimator T_n is consistent estimator for $g(\Theta)$ (a function of Θ) if $E(T_n) = g(\Theta)$ and $V(T_n) \rightarrow 0$ as $n \rightarrow \infty$
- Consistent Estimators need not be unbiased
- Unbiased estimators need not be consistent
- Suppose T_n is a consistent estimator of Θ and $h(\Theta)$ is a continuous function of Θ then $h(T_n)$ is consistent for $h(\Theta)$. Hence consistent possess the invariance property
- If a consistent estimator exists whose sampling variance is less than that of any other consistent estimator it is said to be most efficient and it provides a standard for the measurement of efficiency of a statistic.