

## Summary

- An estimator or estimate is said to be a best estimator or estimate if it is unbiased, consistent, efficient and sufficient
- The amount of bias:  $B = \text{Estimated value} - \text{true value of the parameter}$
- The sample mean  $\bar{x}$  is an unbiased estimator of the population mean
- Generally unbiased estimators does not possess the invariance property
- An estimator is said to be consistent if the variance of its sampling distribution decreases with increasing sample size
- An estimator  $T_n$  is consistent estimator for  $g(\Theta)$  ( a function of  $\Theta$ ) if  $E(T_n) = g(\Theta)$  and  $V(T_n) \rightarrow 0$  as  $n \rightarrow \infty$
- Consistent Estimators need not be unbiased
- Unbiased estimators need not be consistent
- Suppose  $T_n$  is a consistent estimator of  $\Theta$  and  $h(\Theta)$  is a continuous function of  $\Theta$  then  $h(T_n)$  is consistent for  $h(\Theta)$ . Hence consistent possess the invariance property
- If a consistent estimator exists whose sampling variance is less than that of any other consistent estimator it is said to be most efficient and it provides a standard for the measurement of efficiency of a statistic