

# Glossary

**Random Variable** - A random variable is an assignment of numbers to possible outcomes of a random experiment

**Discrete random variable** - A discrete random variable is one whose set of possible values is countable

**continuous random variable** - A quantitative random variable is *continuous* if its set of possible values is uncountable

**Moment generating function** - the **moment-generating function** of a random variable  $X$  is  $M_X(t) = E[e^{tx}]$ , for  $t \in \mathbb{R}$  wherever this expectation exists.

**uniqueness theorem** - The Uniqueness explains moment generating functions uniquely defines the probability distribution of a function of random variables.

**probability distribution** - The probability distribution of a random variable specifies the chance that the variable takes a value in any subset of the real numbers. The probability distribution of a random variable is completely characterized by the cumulative probability distribution function

**probability density function** - The chance that a continuous random variable is in any range of values can be calculated as the area under a curve over that range of values. The curve is the probability density function of the random variable. That is, if  $X$  is a continuous random variable, there is a function  $f(x)$  such that for every pair of numbers  $a \leq b$ ,  $P(a \leq X \leq b) = (\text{area under } f \text{ between } a \text{ and } b)$ ;  $f$  is the probability density function of  $X$

**Distribution** - The distribution of a set of numerical data is how their values are distributed over the real numbers

**Distribution function** - The empirical (cumulative) distribution function of a set of numerical data is, for each real value of  $x$ , the fraction of observations that are less than or equal to  $x$

**joint probability distribution** - If  $X_1, X_2, \dots, X_k$  are random variables defined for the same experiment, their *joint probability distribution* gives the probability of events determined by the collection of random variables: for any collection of sets of numbers  $\{A_1, \dots, A_k\}$ , the joint probability distribution determines  $P(X_1 \text{ is in } A_1 \text{ and } X_2 \text{ is in } A_2 \text{ and } \dots \text{ and } X_k \text{ is in } A_k)$ .

**Transformation technique** – Transformations technique turn set of variables into other set of random variables variables.

**jacobian** - an mathematical term used when changing variables to simplify a region or an integrand.