

## Summary

- A continuous random variable  $x$  is said to follow uniform distribution in the interval  $(a, b)$  if its probability density function is given by,  $f(x)=1/(b-a)$ ,  $0 < x < 1$ , and we write  $x \sim U(a,b)$   
Here  $a$  and  $b$  are the parameters of the distribution
- In particular if  $a=0$  and  $b=\theta$  then we can write,  $x \sim U(0, \theta)$ 
  - If  $a=-\theta$  and  $b=\theta$ , then  $X \sim U(-\theta, \theta)$
  - Hence we can define uniform distribution for any two constants  $a$  and  $b$
  - Mean of the distribution is given by  $(b+a)/2$
  - Variance of the distribution is given by,  $(b-a)^2/12$
  - Moment generating function (mgf) is given by  $(e^{tb}-e^{ta}) / t(b-a)$
  - Median of the distribution is,  $(b+a) / 2$
  - Mean deviation is given by,  $(b-a) / 4$
- For a rectangular distribution with pdf.  $f(x) = 1 / 2a$ ,  $-a < x < a$ , mgf about origin is  $(\sinh at)/at$ . Also we have shown that moments of even order are given by,  $\mu_{2n} = a^{2n}/(2n+1)$
- On the  $x$ -axis,  $(n+1)$  points are taken independently between the origin and  $x=1$ , all positions being equally likely the probability that the  $(k+1)^{th}$  of these points, counted from origin lies in the interval  $x-1/2dx$  to  $x+1/2dx$  is  $\binom{n}{k} (n+1)x^k(1-x)^{n-k} dx$