



## **[Summary]**

### **[Partial Differentiation of Functions of Function and Implicit Function]**

<b>Subject:</b>	Business Economics
<b>Course:</b>	B. A. (Hons.), 6 <sup>th</sup> Semester, Undergraduate
<b>Paper No. &amp; Title:</b>	Paper – 631 Advanced Mathematical Techniques
<b>Unit No. &amp; Title:</b>	Unit – 2 Function of Two Variables
<b>Lecture No. &amp; Title:</b>	Lecture – 2 Partial Differentiation of Functions of Function and Implicit Function

## Summary

- $\frac{\partial u}{\partial x}$  is the change in  $u$  due to a small change in  $x$  keeping  $y$  constant.
- $\frac{dx}{dt}$  denotes the change in  $x$  due to a small unit change in  $t$ .
- $\frac{\partial u}{\partial x} \frac{dx}{dt}$  will be the amount of change in  $u$  due to a small change in  $t$  that is transmitted through  $x$ .
- $\frac{\partial u}{\partial y} \frac{dy}{dt}$  will be the amount of change in  $u$  due to a small change in  $t$  that is transmitted through  $y$ .
- The change in  $u$  due to a small change in  $t$  will be linear sum of these two effects and it is called the total derivative of  $u$  with respect to  $t$ .
- For  $u = f(x,y)$ ,  $x = g(t)$ ,  $y = h(t)$  where  $t$  is the independent variable. The second order total differentiation is given by

$$\frac{d^2 u}{dt^2} = u_{xx} \left( \frac{dx}{dt} \right)^2 + u_{yy} \left( \frac{dy}{dt} \right)^2 + u_x \frac{d^2 x}{dt^2} + u_y \frac{d^2 y}{dt^2} + 2u_{xy} \frac{dx}{dt} \frac{dy}{dt}.$$

- A function is said to be homogeneous function of degree  $n$  if  $f(tx,ty) = t^n f(x,y)$ .
- Euler's Theorem: Let  $u = u(x,y)$  be a homogeneous function of degree  $n$ . Then  $xu_x + yu_y = nu$ .
- Let  $q_a = u(P_a, P_b)$  where  $q_a$  is the quantity of good A demanded,  $P_a$  is its price, and  $P_b$  is the price of good B.

Price elasticity is defined as  $\eta = - \frac{\partial q_a}{\partial P_a} \frac{P_a}{q_a}$ .