

FAQs

1. An RC beam 300mm wide and 700mm deep overall, is reinforced with 3 Nos. of 20mm dia bars. The centres of bars are 50mm from the underside of the beam. The maximum stresses are not to exceed 7 N/mm² for concrete and 190 N/mm² for steel. Find the moment of resistance and the safely distributed load, the beam can carry. The span is 6m.

Solution:

Given

b	=	300mm
D	=	700mm
Effective cover	=	50mm
d	=	700 – 50 = 650mm
A _{st}	=	942mm ²
σ _{cbc}	=	7 N/mm ²
σ _{st}	=	190 N/mm ²
M _r	=	?

To find x_c

$$\frac{\sigma_{cbc}}{x_c} / \frac{\sigma_{st}}{m} = \frac{x_c}{d - x_c}$$
$$x_c = 214.08\text{mm}$$

To find x

$$b \cdot x \cdot \frac{x}{2} = m A_{st} (d - x)$$
$$x = 195.115\text{mm}$$

here $x < x_c$; it is under reinforced section

To find M_r

$$M_r = T \cdot X \cdot z = A_{st} \sigma_{st} (d - x/3)$$
$$M_r = 104.7 \text{ kNm}$$
$$M_r = M = w l^2 / 8 = 104.7 \text{ kNm}$$
$$w = 23.27 \text{ kN/m}$$
$$\text{self wt. of beam} = 0.3 \times 0.7 \times 25 = 5.25 \text{ kN/m}$$
$$\text{Net wt. on beam} = 23.27 - 5.25 = 18.02 \text{ kN/m}$$

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2. An RC beam 250 x 500mm overall in section, is reinforced with four 22mm dia bars at the bottom with a cover of 40mm from the centre of reinforcement. The effective span is 5m. Find the concentrated load the beam can support at the support at the centre. Take σ_{cbc}=5 N/mm² σ_{st}=190 N/mm².

Solution:

Given

$$\begin{aligned} b &= 250\text{mm} \\ D &= 500\text{mm} \\ \text{Effective cover} &= 40\text{mm} \\ d &= 500 - 40 = 460\text{mm} \\ A_{st} &= 1520\text{mm}^2 \\ \sigma_{cbc} &= 5 \text{ N/mm}^2 \\ \sigma_{st} &= 190 \text{ N/mm}^2 \\ M_r &= ? \end{aligned}$$

To find x_c

$$\begin{aligned} \frac{\sigma_{cbc}}{x_c} / \frac{\sigma_{st}}{m} &= \frac{x_c}{d - x_c} \\ x_c &= 156.44\text{mm} \end{aligned}$$

To find x

$$\begin{aligned} \frac{bx \cdot x}{2} &= m A_{st} (d - x) \\ x &= 230\text{mm} \\ \text{here } x &> x_c; \text{ it is over reinforced section} \end{aligned}$$

To find M_r

$$\begin{aligned} M_r &= C \times X \times z = bx \sigma_{cbc} / 2 (d - x/3) \\ M_r &= 58.05 \text{ kNm} \\ \text{Self wt. of beam } w_s &= 0.25 \times 0.5 \times 25 = 3.125 \text{ kN/m} \\ M_s &= w_s l^2 / 8 = 9.765 \text{ kNm} \\ \text{Net Moment } M &= 58.05 - 9.765 = 48.285 \text{ kNm} \\ M &= 48.285 = wl/4 \\ \text{Net load on beam } w &= 38.628 \text{ kN.} \end{aligned}$$

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3. The cross section of a rectangular beam has to resist a bending moment of 75 kNm. If the beam is 250mm wide and the permissible stresses in concrete and steel are 5 N/mm² and 190 N/mm² respectively, find the effective depth and tensile reinforcement required.

Solution:

Given

$$\begin{aligned} M_r &= 75 \text{ kNm} \\ b &= 250\text{mm} \\ \sigma_{cbc} &= 5 \text{ N/mm}^2 \\ \sigma_{st} &= 190 \text{ N/mm}^2 \\ d &= ? \\ A_{st} &= ? \end{aligned}$$

Assuming a balanced section

To find x_c

$$\sigma_{cbc} / \sigma_{st} / m = x_c / d - x_c$$

$$x_c = 0.329d$$

$$z = (d - x_c/3) = 0.89d$$

To find d

$$M_r = C X z = b x \sigma_{cbc} / 2 (d - x_c/3)$$

$$M_r = 183.86d^2 = 75 \text{ kNm}$$

$$d = 639.22 \text{ mm} = 640 \text{ mm}$$

To find A_{st}

$$M_r = T X z = A_{st} \sigma_{st} (d - x_c/3)$$

$$A_{st} = 693 \text{ mm}^2$$