

FAQs

1. An RC beam 300mm x 500mm effective, is reinforced with 804mm² and 1520mm² of steel at the top and bottom respectively. Find the M_U the beam using M20 and Fe415 as materials. $d' = 33$ mm.

To find $x_{u,lim}$

$$\begin{aligned}x_{u,lim} &= 0.479d \\x_{u,lim} &= 239.50\text{mm}\end{aligned}$$

To find strain at d' from top

$$\begin{aligned}\text{Strain at } d' \text{ from top} &= 0.0035 (x_{u,lim} - d') / x_{u,lim} \\&= 0.00302\end{aligned}$$

To find stress f_{sc} at d' from top

$$f_{sc} = 354.08 \text{ N/mm}^2$$

To find stress f_{cc} at d' from top

$$\begin{aligned}f_{cc} &= 0.446 f_{ck} \\&= 8.92 \text{ N/mm}^2\end{aligned}$$

To find M_U

$$M_U = 0.36f_{ck}x_{u,lim}b (d - 0.416x_{u,lim}) + A_{sc} (f_{sc} - f_{cc}) (d - d')$$

$$M_U = 181.14 \text{ kNm.}$$

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2. An RC beam 200mm x 300mm effective, is constructed with M20 and Fe415 as materials. $d' = 30$ mm. Find the steel required, of the factored moment on beam is 74kNm.

To find $M_{u,lim}$

$$\begin{aligned}M_{u,lim} &= 0.138f_{ck}bd^2 \\M_{u,lim} &= 49.68 \text{ kNm}\end{aligned}$$

Here $M_u > M_{u,lim}$; hence it is doubly reinforced section.

To find A_{st1} required for a balanced section

$$\begin{aligned}A_{st1} &= 0.36f_{ck}b x_{u,lim} / 0.87f_y \\A_{st1} &= 573.31 \text{ mm}^2\end{aligned}$$

To find M_{u1}

$$\begin{aligned}
 M_{u1} &= M_u - M_{ulim} \\
 &= \mathbf{24.32 \text{ kNm}}
 \end{aligned}$$

To find A_{st2}

$$\begin{aligned}
 M_{u1} &= \mathbf{0.87 f_y A_{st2} (d - d')} \\
 A_{st2} &= \mathbf{249.975 \text{ mm}^2}
 \end{aligned}$$

To find total A_{st}

$$A_{st} = 822.61 \text{ mm}^2$$

To find strain at d^1 from top

$$\begin{aligned}
 \text{Strain at } d^1 \text{ from top} &= \mathbf{0.0035 (x_{u,lim} - d^1) / x_{u,lim}} \\
 &= \mathbf{0.002769}
 \end{aligned}$$

To find stress f_{sc} at d^1 from top

$$f_{sc} = \mathbf{353 \text{ N/mm}^2}$$

To find stress f_{cc} at d^1 from top

$$\begin{aligned}
 f_{cc} &= \mathbf{0.446 f_{ck}} \\
 &= \mathbf{8.92 \text{ N/mm}^2}
 \end{aligned}$$

To find A_{sc}

$$\begin{aligned}
 M_{u1} &= \mathbf{A_{sc} (f_{sc} - f_{cc}) (d - d')} \\
 A_{sc} &= \mathbf{261.78 \text{ mm}^2}
 \end{aligned}$$