

FAQ's

1. Write the shear equation and explain the terms?

$$q = \frac{F A \bar{y}}{I b}$$

Where,

q = Shear stress

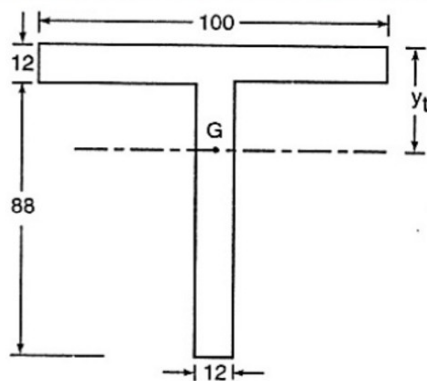
A = Area of the beam above the layer considered

Y = Distance between neutral axis and the centre of gravity of area A

I = Moment of inertia

B = Width of section

2. Draw the shear stress distribution diagram of the given beam subjected to a shear force of 20kN?



Let y be the distance of C.G. from top fibre. Then taking moment of area about top fibre and dividing it by total area we get

$$y_t = \frac{(100 \times 12 \times 6 + 12 \times 88(44 + 12))}{(100 \times 12 + 88 \times 12)} \\ = 29.404 \text{ mm}$$

Moment of inertia about neutral axis,

$$I = \frac{(100 \times 12^3)}{12} + (100 \times 12(29.404 - 6)^2) + \frac{(12 \times 88^3)}{12} \\ + (12 \times 88(56 - 29.404)^2) \\ = 2100127.3 \text{ mm}^4$$

Shear stress at bottom of the flange

$$\text{Area above this level} = 100 \times 12 = 1200 \text{ mm}^2$$

$$\text{c.g. of this area from neutral axis} = y_t - 6 = 23.404 \text{ mm}$$

$$\text{width at this level} = 100 \text{ mm}$$

$$q_b = 20 \times 10^3 \times (1200 \times 23.404) / (100 \times 2100127.3)$$

$$= 2.675 \text{ N/mm}^2$$

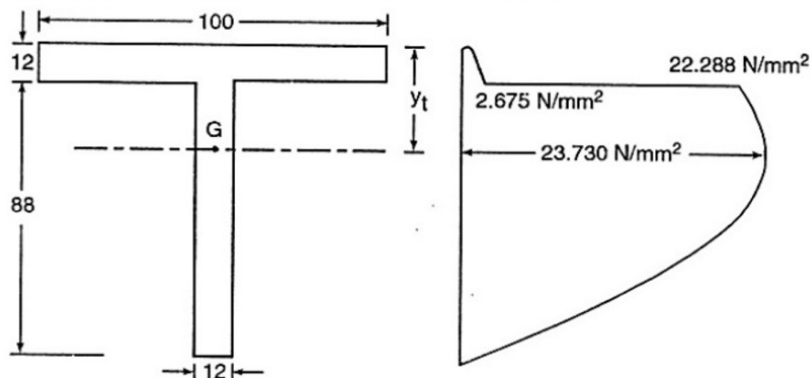
At web,

$$q_w = 20 \times 10^3 \times (1200 \times 23.404) / (12 \times 2100127.3) \\ = 22.299 \text{ N/mm}^2$$

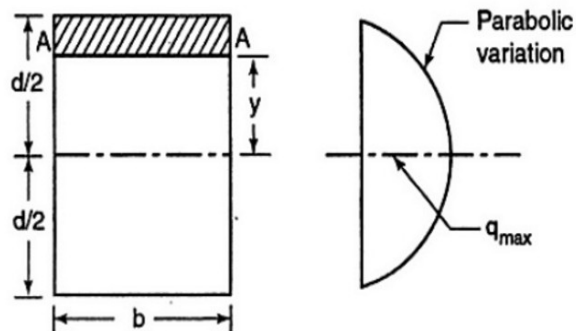
At neutral axis,

$$I = (12 \times 100 \times (29.404 - 6)) + 12 \times (29.404 - 12) \times ((29.404 - 12) / 2) \\ = 29902.195 \text{ mm}^4 \\ q_n = 20 \times 10^3 \times 29902.195 / 12 \times 2100127.3 \\ = 23.730 \text{ N/mm}^2$$

The shear stress distribution is given below



3. Draw the shear stress distribution of the rectangular section and state the difference between average shear stress and maximum shear stress?



Shear stress,

$$q = F A y / I \\ = (F \times b \times ((d/2) - y) \times 0.5 \times ((d/2) + y)) / (b \times b d^3 / 12) \\ = 6F((d^2/4) - y^2) / (b d^3)$$

i.e, shear stress varies parabolically

When $y = d/2$, $q = 0$

When $y = 0$, $q = \text{maximum}$

$$q_{\max} = 6F d^2 / 4 b d^3 = 1.5F / b d = 1.5 q_{\text{avg}}$$

Therefore the maximum shear stress is 1.5 times greater than the average shear stress for a rectangular section.