

FAQ's

1. Solve the system of equations

$$(D-1)x + Dy = 2t + 1 \dots\dots\dots (1)$$

$$(2D+1)x + 2Dy = t \dots\dots\dots (2)$$

Solution:

Subtracting twice equ(1) from (2) we have $3x = 3t - 2$.

Substituting $x = -t - \frac{2}{3}$ in (1) we obtain $Dy = 2t + 1 - (D-1)x = t + \frac{4}{3}$ and

$$y = \frac{1}{2}t^2 + \frac{4}{3}t + c_1$$

2. Solve $(x^3D^3 + 3x^2D^2 - 2xD + 2)y = 0$

Solution:

The transformation $x = e^z$ reduces the equation to $\{D(D-1)(D-2) + 3D(D-1) - 2D + 2\}y = (D^3 - 3D + 2)y = 0$

Whose solution is $y = c_1e^z + c_2ze^z + c_3e^{-2z}$ since $z = \ln x$, the complete solution

of the given equation is $y = c_1(x) + c_2(x) \ln x + \frac{c_3}{x^2}$

3. In the differential equation of the form $F(D)y = Q$ if Q is of the form e^{ax} how the particular integral is obtained?

Solution:

If Q is of the form e^{ax}

$$y = \frac{1}{F(D)} e^{ax} = \frac{1}{F(a)} e^{ax}, F(a) \neq 0$$

4. Give the Cauchy linear equations.

Solution:

The Cauchy linear equation is

$$p_0x^n \frac{d^n y}{dx^n} + p_1x^{n-1} \frac{d^{n-1} y}{dx^{n-1}} + p_2x^{n-2} \frac{d^{n-2} y}{dx^{n-2}} + \dots\dots\dots p_{n-1}x \frac{dy}{dx} + p_n y = Q(x)$$

in which $p_0, p_1, p_2, \dots\dots\dots p_n$ are constants.

5. Give the Legendre linear equation.

Solution:

The Legendre linear equation is

$$p_0(ax+b)^n \frac{d^n y}{dx^n} + p_1(ax+b)^{n-1} \frac{d^{n-1} y}{dx^{n-1}} + \dots + p_{n-1}(ax+b) \frac{dy}{dx} + p_n y = Q(x)$$