

### FAQ's

1. In a right angle triangle ABC  $\tan A = \frac{3}{4}$  find  $\sin A$  and  $\cos A$

**Answer:**

We know that  $\tan A = \frac{\sin A}{\cos A}$  and  $\tan A = \frac{\text{adjacent}}{\text{opposite}} = \frac{3}{4}$  so in a right angle triangle adjacent side=3 and opposite side=4.

So according to **pythagorous** theorem hypotenuse=5 so

$$\sin A = \frac{\text{opposite side}}{\text{hypotenuse}} = \frac{4}{5} \quad \cos A = \frac{\text{adjacent side}}{\text{hypotenuse}} = \frac{3}{5}$$

2. Calculate  $\cos\left(\frac{\pi}{6}\right)$

**Answer:**

To calculate the value of the cosine  $\left(\frac{\pi}{6}\right)$  at  $30^\circ$ , construct a  $30^\circ$ - $60^\circ$ - $90^\circ$  right angle i.e a triangle with sides

1.  $\sqrt{3}$ , and

2. Then  $\cos\left(\frac{\pi}{6}\right) = \frac{\sqrt{3}}{2}$

3. Calculate  $\tan -\left(\frac{\pi}{6}\right)$

**Answer:**

$$\text{By definition } \tan \theta = \frac{\sin \theta}{\cos \theta} \text{ now } \tan -\left(\frac{\pi}{6}\right) = \frac{\sin -\left(\frac{\pi}{6}\right)}{\cos -\left(\frac{\pi}{6}\right)} = \frac{-\sin\left(\frac{\pi}{6}\right)}{\cos\left(\frac{\pi}{6}\right)} \text{ To}$$

calculate the sine and cosine functions at  $\theta = \left(\frac{\pi}{6}\right)$  (i.e  $30^\circ$ ) construct  $30^\circ$ - $60^\circ$ -

90° right triangle i.e a triangle with sides 1,  $\sqrt{3}$ , and 2. Then  $\cos$

$$\left(\frac{\pi}{6}\right) = \frac{1}{2} \text{ and } \cos\left(\frac{\pi}{6}\right) = \frac{\sqrt{3}}{2} \text{ which implies that } \tan\left(\frac{\pi}{6}\right) = \frac{\frac{1}{2}}{\frac{\sqrt{3}}{2}} = \frac{1}{\sqrt{3}}$$

4. Prove that  $(\sin x + \cos x)^2 = 1 + \sin 2x$

**Answer:**

$$\begin{aligned} (\sin x + \cos x)^2 &= \sin^2 x + 2\sin x \cos x + \cos^2 x \\ &= 1 + 2\sin x \cos x = 1 + \sin 2x \end{aligned}$$

5. Given  $\sin^2 x + \cos^2 x = 1$ , prove that  $1 + \cot^2 x = \operatorname{cosec}^2 x$

**Answer:**

$$\sin^2 x + \cos^2 x = 1$$

$$\frac{\sin^2 x + \cos^2 x}{\sin^2 x} = \frac{1}{\sin^2 x}$$

$$1 + \frac{\cos^2 x}{\sin^2 x} = \frac{1}{\sin^2 x}$$

$$1 + \cot^2 x = \operatorname{cosec}^2 x$$